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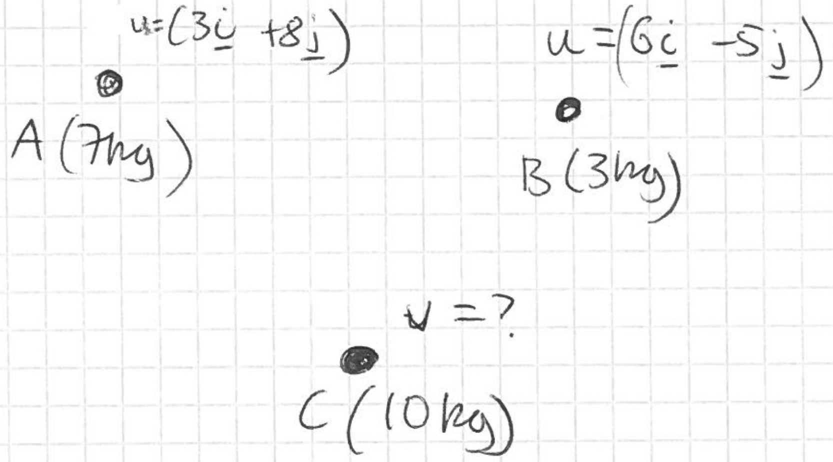
Jan 2012 M1 Written Solutions

(1) Before

After



mv before = mv after.

$$7(3\underline{i} + 8\underline{j}) + 3(6\underline{i} - 5\underline{j}) = 10(x\underline{i} + y\underline{j})$$

$$(21 + 18)\underline{i} + (56 - 15)\underline{j} = 10x\underline{i} + 10y\underline{j}$$

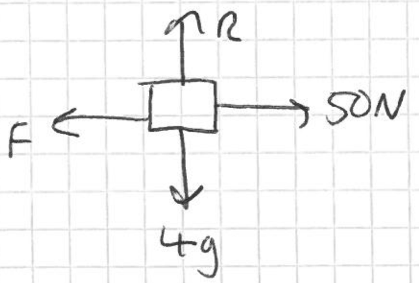
$$39\underline{i} + 41\underline{j} = 10x\underline{i} + 10y\underline{j}$$

so $39 = 10x \Rightarrow x = 3.9$

$41 = 10y \Rightarrow y = 4.1$

$$v = 3.9\underline{i} + 4.1\underline{j}$$

(2) (a)



(b) vertical forces balanced

so $R = 4g = 39.2\,N$

(c) Use NII ($F = ma$).

$50 - F = 4 \times 3$

$50 - 12 = F$

so $F = 38\,N$

(d) Using $F = \mu R$

$\mu = \frac{F}{R} = \frac{38}{39.2} = 0.969$

(e) friction would be less (a is the same so net force is the same) so μ would be smaller

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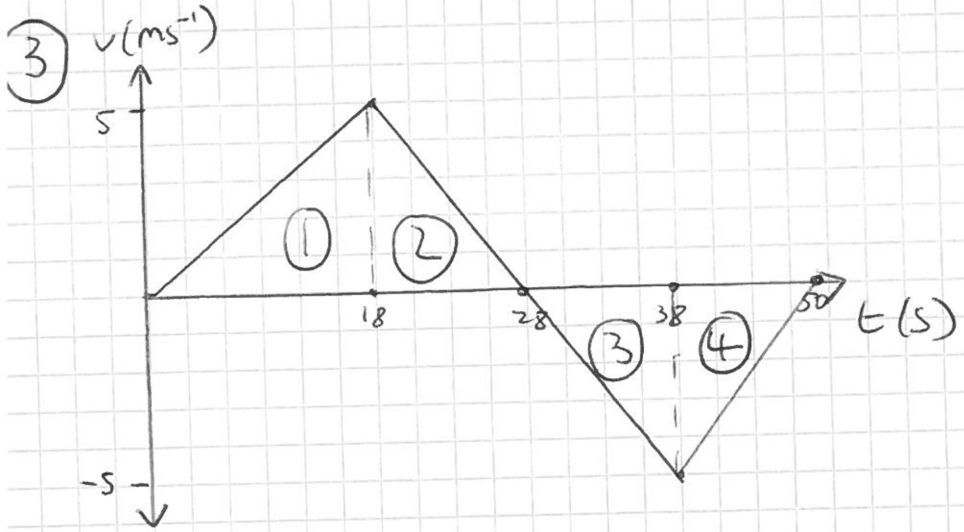


(a) Area under so 1 + 2

$1 = \frac{18 \times 5}{2} = 45m$ $\quad 2 = \frac{10 \times 5}{2} = 25m$

$45 + 25 = \underline{\underline{70m}}$

(b) 1 + 2 + 3 + 4 (Notice → distance not displacement)

$70 + \frac{10 \times 5}{2} + \frac{12 \times 5}{2}$

$70 + 25 + 30 = \underline{\underline{125m}}$

(c) average speed $= \frac{\text{total distance}}{\text{total time}} = \frac{125}{50} = \underline{\underline{2.5ms^{-1}}}$

(d) displacement

1 and 2 are in same direction so

70m in this direction

3 + 4 = 55 is in opposite direction

so $70 - 55 = \underline{\underline{15 m}}$

(e) average velocity $= \frac{\text{total displacement}}{\text{total time}} = \frac{15}{50} = 0.3ms^{-1}$

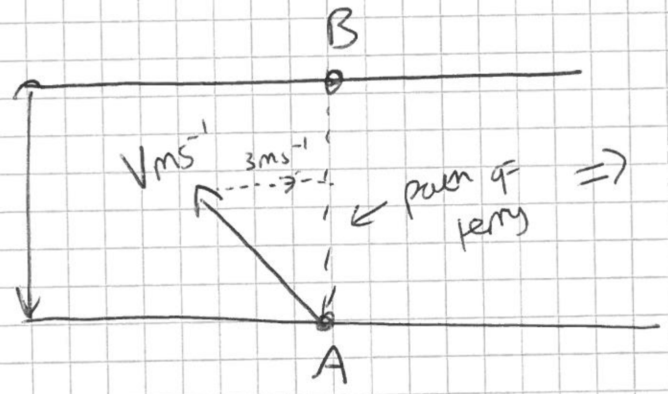
(f) acceleration is gradient i.e. $a = \frac{\Delta v}{t} = \frac{[illegible]}{18}$

$= 0.27$[illegible]

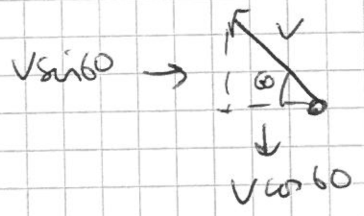
$= 0.28\,ms$[illegible]

(2SF)

(4)



$\Rightarrow$ ferry has no horizontal displacement so resultant velocity horizontally must be $0 ms^{-1}$



so $V\cos 60 = 3$

$V = \frac{3}{\cos 60} = 6 ms^{-1}$

(b) Only need vertical velocity & displacement

so velocity $= V\sin 60 = 6\sin 60$

displacement $= 200$

so $t = \frac{200}{6\sin 60} = 38.49$

so **38 s**

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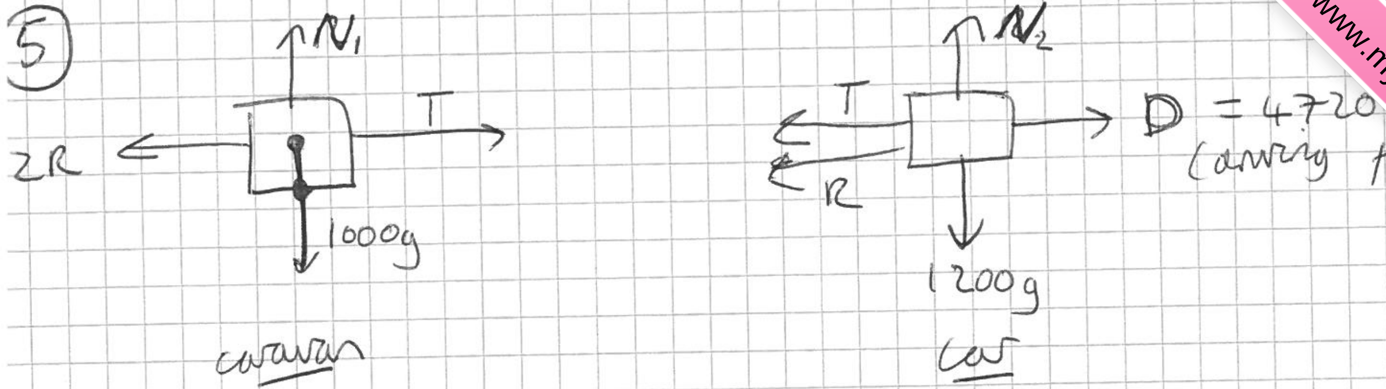

$$a = 1.6\ ms^{-2}$$

(a) Use NII $F = ma$ on each:

car: $D - T - R = 1200 \times 1.6$

$4720 - T - R = 1920$ (1)

caravan: $T - 2R = 1000 \times 1.6$

$T - 2R = 1600$ (2)

(1) + (2) to cancel T gives

$$4720 - 3R = 3520$$

$$3R = 1200$$

$$\Rightarrow R = \underline{\underline{400N}}$$

(b) Use (2) $T - 2(400) = 1600$

$$T = 1600 + 800 = \underline{\underline{2400N}}$$

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6 a(i) $V^2 = u^2 + 2as \Rightarrow a = \dfrac{V^2 - u^2}{2s}$

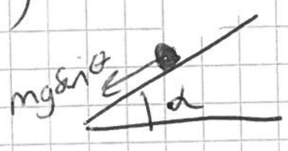
$a = \dfrac{10^2 - 4^2}{2 \times 50} = \dfrac{100 - 16}{100} = 0.84\,ms^{-2}$

(ii) $V = u + at \Rightarrow t = \dfrac{V - u}{a} = \dfrac{10 - 4}{0.84} = \dfrac{6}{0.84}$

$= 7.14\,s$

(b) $F = ma = 70 \times 0.84 = 58.8\,N$

c(i)



free-wheeling, no resistive forces

so $mg\sin\theta$ = net force

↓

only forces parallel to slope considered

$70g\sin\theta = 58.8$

$\sin\theta = 0.0857142$

$\theta = 4.9171$

$= 4.92^\circ$

(ii) Now net force is $mg\sin\theta - 30$

so $70g\sin\theta - 30 = 58.8$

$\sin\theta = \dfrac{58.8 + 30}{70g} = 0.129446$

$\theta = 7.43758$

$\theta = 7.44^\circ$

(d) the cyclist is accelerating and resistive forces would vary (increase) with the speed so a constant resistive force is unrealistic.

7 (a) $a = 4.2\underline{i} + 2.5\underline{j}$ $t = 20s$

consider $\underline{j}$ only for (a) (finding height)

vertically

$s = ?$
$u = 0$
v
$a = 2.5$
$t = 20$

$s = ut + \frac{1}{2}at^2$
$= 0 + \frac{1}{2} \times 2.5 \times 20^2$
$= 500m$

(b) $V = u + at$
$= 0 + (4.2\underline{i} + 2.5\underline{j}) \times 20 = (84\underline{i} + 50\underline{j})\ ms^{-1}$

(c) Find time when $\underline{j}$ component of $\underline{s}$ is 180

$s_y = ut + \frac{1}{2}at^2$
$= 0 + \frac{1}{2} \times 2.5 \times t^2$ ← vertical component only so $a = 2.5\underline{j}$
$= 1.25t^2$

$180 = 1.25t^2 \Rightarrow t^2 = 144$ $t = +12s$

(−12s makes no sense)

So $V = u + at$
$= (4.2\underline{i} + 2.5\underline{j}) \times 12 = 50.4\underline{i} + 30\underline{j}$

so speed $= \sqrt{50.4^2 + 30^2} = 58.6529$

$= 58.7ms^{-1}$ (3SF)

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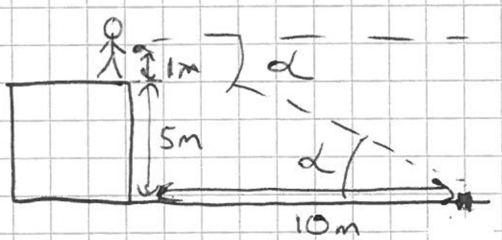
(a)



$\tan\alpha = \left(\frac{5+1}{10}\right)$ $\qquad \alpha = \tan^{-1}\left(\frac{6}{10}\right) = 30.9638$

$\alpha = 30.1$ (3SF)

(b) $s_y = -6$

$s_y = ut\sin\theta - \frac{1}{2}gt^2$

$-6 = 8\sin(-30.9638)t - 4.9t^2$

use $-\alpha$ as angle is below horizontal

$4.9t^2 + 4.11597t - 6 = 0$

use quadratic formula

$\frac{-b \pm \sqrt{b^2-4ac}}{2a}$

$t = 0.76359$

or $t = -1.60359$

so $\underline{t = 0.764\text{ s}}$

(c) Find s_x when $t = 0.76359$

$s_x = ut\cos\theta = 8 \times 0.76359 \times \cos(-30.9638)$

$= 5.23818$

so $10 - 5.23818 = 4.76182$

$= \underline{4.76\text{ m}}$ (3SF)

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